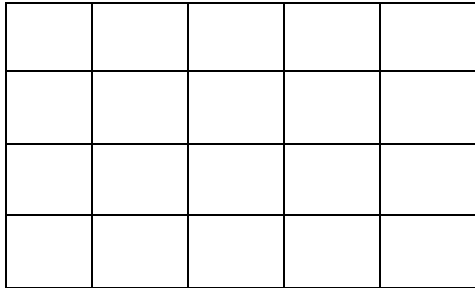


Example
Individual problem

Problem

The figure below is made up of 20 Rectangles.
How many rectangles (of all sizes) are there altogether in the figure?



So lotion

Write the numbers “1”to”5”in the rectangles on the first row.
Write the numbers “2”to”10” in the rectangles on the second row.
Write the numbers “3”to”15” in the rectangles on the third row.
Write the numbers “4”to”20” in the rectangles on the fourth row.

Add up all the numbers to get the sum of 150

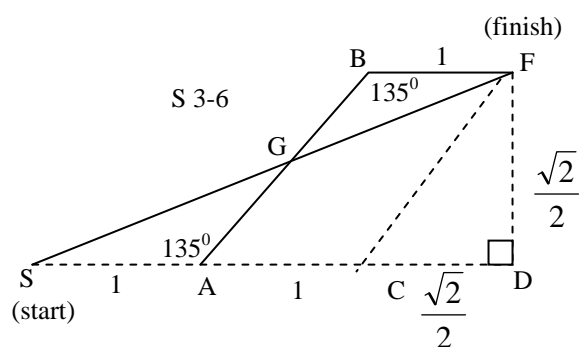
4	8	12	16	20
3	6	9	12	15
2	4	6	8	10
1	2	3	4	5

Answer: 150

Example
Individual problem

Problem

A man walks one mile east, then one mile northeast, then another mile east (Fig. S3-6). Find the distance, in miles, between the man's initial and final positions.



Solution

Let S and F be the starting and finishing positions, respectively.

Draw $\overline{FD} \perp \overline{SA}$, then draw $\overline{FC} \parallel \overline{AB}$.

In rhombus $ABFC$, $CF = BF = AC = 1$ (#21-1); also $AS = 1$.

In isosceles right $\triangle FDC$, $FD = CD = \frac{\sqrt{2}}{2}$ (#55b).

Applying the Pythagorean Theorem (#55) to right $\triangle DSF$,

$$\begin{aligned} (FD)^2 + (SD)^2 &= (SF)^2 \\ \left(\frac{\sqrt{2}}{2}\right)^2 + \left(2 + \frac{\sqrt{2}}{2}\right)^2 &= (SF)^2 \end{aligned}$$

$$\sqrt{5 + 2\sqrt{2}} = SF.$$

Example Team problem

Problem

A bag contains two red cabbages and three green cabbages. Tracy, who is blindfolded, randomly selects one of the cabbages and places it in an empty pan. Then she randomly selects a second cabbage from those remaining in the bag and also places that in the pan. What is the percentage likelihood that of the two cabbages that are now in the pan, one is red and the other is green?

So lotion

Method 1: from first principles.

We name the cabbages R_1, R_2 (the red cabbages) and G_1, G_2, G_3 (the green cabbages).

There are twenty possible selections of two cabbages from the set:

R_1R_2	R_2R_1	G_1R_1	G_2R_1	G_3R_1
R_1G_1	R_2G_1	G_1R_2	G_2R_2	G_3R_2
R_1G_2	R_2G_2	G_1G_2	G_2G_1	G_3G_1
R_1G_3	R_2G_3	G_1G_3	G_2G_3	G_3G_2

All twenty selections are equally likely and twelve of them involve one cabbage of each colour.

So the percentage likelihood is $\frac{12}{20} \times 100\% = 60\%$

Method 2: for those who know something of the theory of probability.

$$\begin{aligned}
 & \text{Prob.} \begin{pmatrix} \text{one red} \\ \text{and} \\ \text{one green} \end{pmatrix} \\
 &= \text{Prob.} \begin{pmatrix} \text{first is red} \\ \text{and} \\ \text{second is green} \end{pmatrix} + \text{Prob.} \begin{pmatrix} \text{first is green} \\ \text{and} \\ \text{second is red} \end{pmatrix} \\
 &= \text{Prob.} \begin{pmatrix} \text{first} \\ \text{is} \\ \text{red} \end{pmatrix} \times \text{Prob.} \begin{pmatrix} \text{second is green} \\ \text{given that} \\ \text{first is red} \end{pmatrix} \\
 &+ \text{Prob.} \begin{pmatrix} \text{first} \\ \text{is} \\ \text{green} \end{pmatrix} \times \text{Prob.} \begin{pmatrix} \text{second is red} \\ \text{given that} \\ \text{first is green} \end{pmatrix} \\
 &= \frac{2}{5} \times \frac{3}{4} \times \frac{3}{5} \times \frac{2}{4} = \frac{12}{20}.
 \end{aligned}$$

So the percentage likelihood is $\frac{12}{20} \times 100\% = 60\%$.

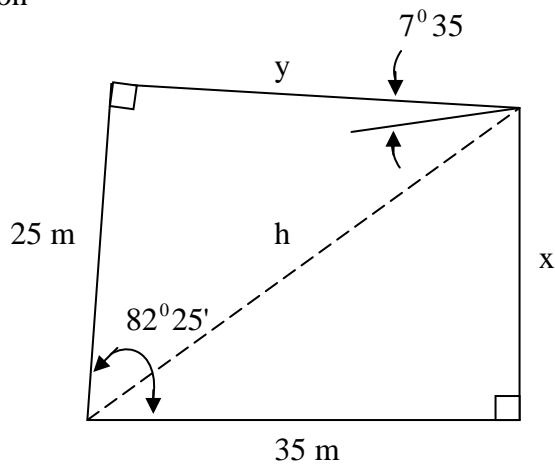
Example
Team problem

Problem

Me Board, April 1981

A corner lot of land is 35m on one street and 25 m on the other street, the angle between the two lines of the street being $82^{\circ} 25'$. The other two lines of the lot are respectively perpendicular to the lines of the streets. What is the worth of the lot at 180 per sq. m

Solution



By Pythagorean Theorem:

$$x^2 + (35m)^2 = h^2$$

$$y^2 + (25m)^2 = h^2$$

$$\therefore x^2 + 1225 = y^2 + 625$$

$$y^2 = x^2 + 600 \dots \dots \dots (1)$$

$$25 \sin 82^{\circ} 25' = x + y \sin 7^{\circ} 35'$$

$$24.781 = x + 0.132y \dots \dots \dots (2)$$

From (2) . $x = .24.781 - 0.132y$

Thus. $y^2 = (24.781 - 0.132y)^2 + 600$

$$y^2 = 614.098 - 6.542y + 0.0174y^2 + 600$$

$$0.9826y^2 + 6.542y - 1214.098 = 0$$

$$y^2 + 6.6578y - 1235.6 = 0$$

By Quadratic Formula:

$$y = \frac{-6.6578 + \sqrt{(6.6578)^2 - 4(-1235.6)}}{2}$$

$$y = 31.98m$$

Thus $x = 24.781 - 0.132(31.98)$

$$= 20.56m$$

$$\begin{aligned}\text{Also, } x &= \sqrt{y^2 - 600} \\ &= \sqrt{(31.98)^2 - 600} \\ &= 20.56m\end{aligned}$$

Therefore, The total area of the lot is

$$\begin{aligned}A &= \frac{1}{2}(25m)y + \frac{1}{2}(35m)x \\ &= \frac{1}{2}(25m)(31.98m) + \frac{1}{2}(35m)(20.56m) \\ &= 759.55sq.m\end{aligned}$$

Therefore, shaded area

$$\begin{aligned}A &= \frac{1}{2}(225\pi) - 180 \\ &= 173.43cm^2 \quad \text{ans.}\end{aligned}$$

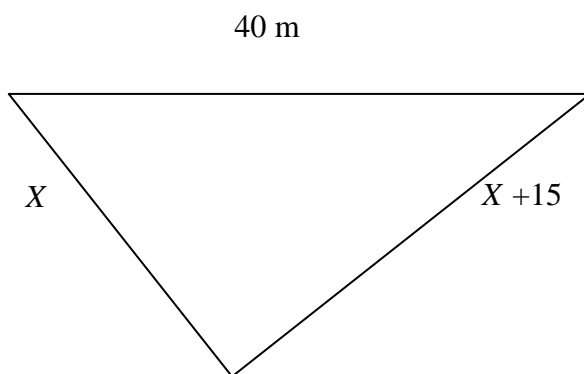
Problem

Me Board, April 1991

A mason was asked to compute the number of hollow blocks. Which have to be purchased to fence one side of a triangular lot in which the two other sides have already been fenced by adjoining lot owners. One of the fenced sides is 40 m long and the other is m longer than the side to be fenced. If the total length of the three sides is 125 m, the height of the fence required is 2436 mm and the length of each hollow block is 406 mm while the width is 203 mm, find the number of hollow blocks that have to be purchased, allowing an additional 10% for breakages. Disregard the effect of posts on the required number of hollow blocks.

Solution:

Let x = length of side to be fenced.



$$\begin{aligned}\text{Perimeter. } P &= x + x + 15 + 40 \\ 125 \text{ m} &= 2x + 55m \\ \therefore x &= \frac{125 - 55}{2} = 35m\end{aligned}$$

Total area of fence

$$\begin{aligned}&= 35,000 \text{ mm} \times 2436 \text{ mm} \\ &= 85,260,000 \text{ mm}^2\end{aligned}$$

$$\begin{aligned} \text{Area of one hollow block} \\ &= 203\text{mm} \times 406\text{mm}, \\ &= 82\,418 \text{ mm}^2 \end{aligned}$$

$$\begin{aligned} \text{Number of hollow blocks needed} \\ &= \frac{85\,260\,000}{82\,418} \\ &= 1034.48 \end{aligned}$$

$$\begin{aligned} \text{With 10\% allowance for breakages, number of hollow blocks to be ordered} \\ &= (1 + 10\%)1034.48 \\ &= 1138 \text{ pieces} \quad \text{ans.} \end{aligned}$$